

$$Q = \frac{\Delta P}{R} \cdot \frac{A}{8\mu L} \quad GFR = 125 \text{ ml/min}$$

Diagram illustrating the calculation of Glomerular Filtration Rate (GFR). The formula is $Q = \frac{\Delta P}{R} \cdot \frac{A}{8\mu L}$. The variables are circled in red: Q , ΔP , R , and $8\mu L$.

$$R = 100 - 200 \text{ } \text{\AA}$$

$$L = 400 - 600 \text{ } \text{\AA}$$

$$\Delta P = 60 - 80 \text{ mm Hg.}$$

$$\mu = 4 \text{ Poise}$$

$$Q_{in} = 1200 \text{ ml/min}$$



$$\frac{dQ}{dx} = -K S \underbrace{P_{UF}}_2$$

$$P_{UF} = (P_C - P_B) - (\Pi_C - \Pi_B)$$

Π = pressione osmotica colloidale

$$\Pi_B \approx 0$$

$$P_{UF} = \Delta p - \Pi_C$$

C differito al volume di

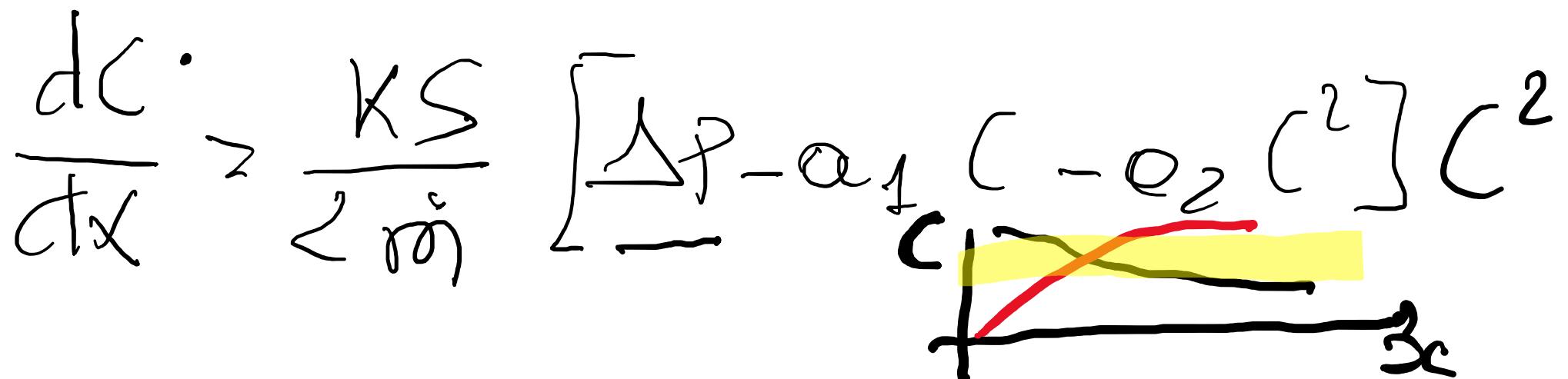
$$\Pi_C = a_1 C + a_2 C^2$$

$$C = \frac{m}{Q} \rightarrow Q = \frac{m}{C}$$

$$\frac{dQ}{dx} = \frac{d}{dx} \left(\frac{m}{C} \right) = -\frac{m}{C^2} \frac{dc}{dx}$$

$$\frac{dQ}{dx} = - \underbrace{KS P_{UF}}_I = - \frac{KS}{I} [\Delta p - \bar{\pi}_C] = - \frac{KS}{I} [\Delta p - \alpha_1(-\alpha_2 C)]$$

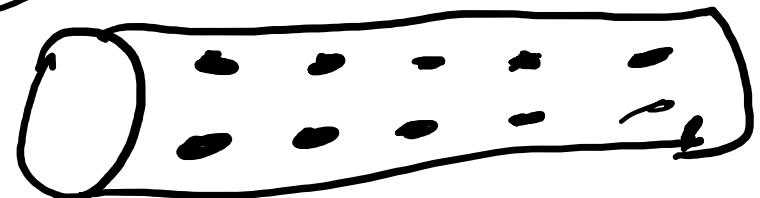
$$-\frac{\dot{m}}{C^2} \frac{dC}{dx} = - \frac{KS}{I} [\Delta p - \alpha_1(-\alpha_2 C)]$$



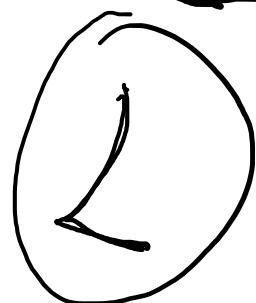
$$C = C_i(\text{Sangue}) - C_i(\text{Urina})$$



S_{min} nelle Superficie dei pori = porosità



angiografia radiopaca
al condotto vas



K

$$= \frac{\Delta C}{\Delta t}$$

process.	HenzG	DISTAG	COLLEGTORE
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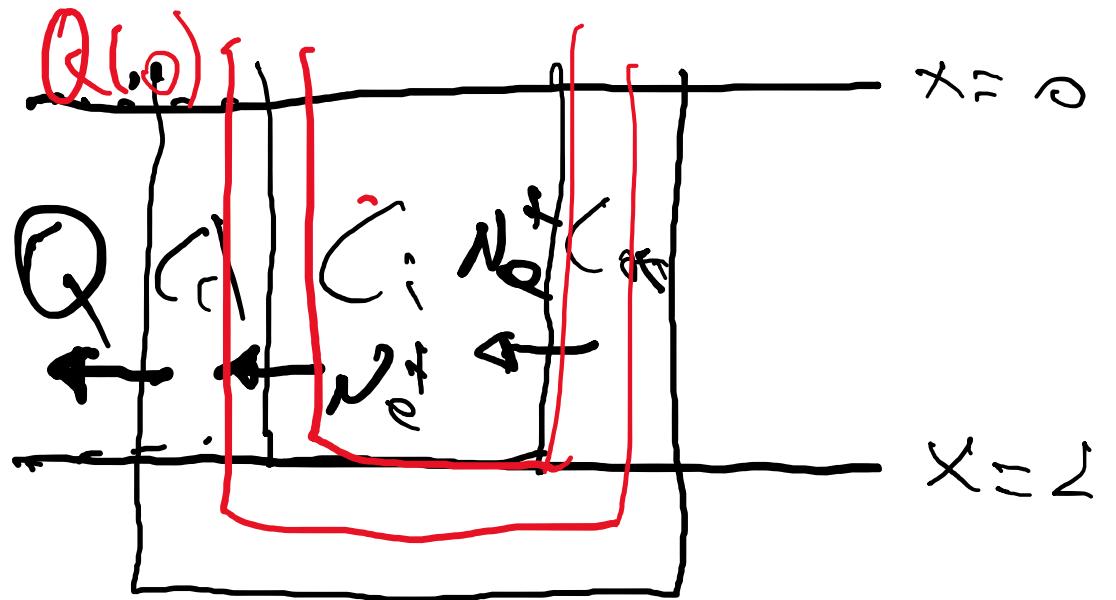
$$\frac{d(Q_{ws}(ij))}{dx_j} = -2\pi R_j J_{ij}$$

$$J_w = K_w Q_w x$$

$$\underline{J}_{NQ} = \overline{K}_{NQ} [C_{NQi} - C_{NQ0}]$$

→ per clona

$$\underline{J}_{NQ} = \overline{K}_{NQ} C_{NQi}$$



$$L = 1 \text{ cm}$$

C_i : concentrazione interstiziale

C_a : conc. nel frotto ascendente

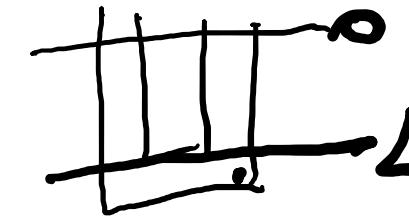
C_d : conc. nel frotto discendente

$$-\frac{d(Qcd)}{dx} = K_d(C_d - C_i) [1]$$

$$Q_Q \frac{d(C_a)}{dx} = K_Q(C_a - C_i) [2] \quad K_Q a = -K_d(C_d - C_i) [4]$$

$$-\frac{dQ}{dx} = K_Q(C_i - C_d) [3]$$

$$Q(0) = 125 \frac{\text{ml}}{\text{min}} = \text{GFR}$$

$$Q_a \frac{d(\alpha)}{dx} = K_a \alpha \quad \xrightarrow{\text{Eq. 2.}} \quad \frac{d\alpha}{\alpha} = \frac{K_a}{Q_a} dx$$


$$\int \frac{d(\alpha)}{\alpha} = \frac{K_a}{Q_a} \int dx \quad \Rightarrow \quad \left[\begin{array}{l} \alpha(x) \\ \alpha(0) \end{array} \right] \frac{d\alpha}{\alpha} = \frac{K_a}{Q_a} \int_0^x dx$$

$$\ln \left(\frac{\alpha(x)}{\alpha(0)} \right) = \frac{K_a}{Q_a} x \quad \Rightarrow \quad \ln \frac{\alpha(x)}{\alpha(0)} = \frac{K_a}{Q_a} x$$

$$\alpha(x) = \alpha(0) e^{\frac{K_a}{Q_a} x}$$

$$-\frac{dQ}{dx} = K_d(C_i - C_d) \quad \text{eq. 3-} \quad K_a Q = -K_d(C_d - C_i) = K_d[C_i - C_d]$$

$$C_i - C_d = \frac{K_a C_a}{K_d}$$

$$-\frac{dQ}{dx} = \frac{K_o K_a C_a}{K_d}$$

$$-\frac{dQ}{dx} = \frac{K_o K_a}{K_d} C_a dx \Rightarrow -\int_{Q(0)}^{Q(x)} dQ = \frac{K_o K_a}{K_d} \int_0^x C_a dx$$

$$Q(x) - Q(0) = \frac{K_o K_a}{K_d} C_a \frac{Q_a}{K_a} \left[e^{\frac{K_a}{Q_a} x} - 1 \right]$$

$$Q(x) = Q(0) - \frac{K_d}{K_a} C_{00} Q_a e^{\frac{K_a}{K_d} x} - 1$$

GFR

$$K_a = -K_d (G_i - i) + x$$

$$K_a(0) = -K_d [d(0) - i(0)] \quad x = \phi$$

$$C_a(0) = -\frac{K_d}{K_a} [d(0) - i(0)] \quad i(0) \geq \phi$$

Eq. d

$$-\frac{d(Q_c d)}{dx} = K_d (C_d - C_i) \quad K_a C_a = -K_d (C_d - C_i)$$

$$+\frac{d(Q_c d)}{dx} = +K_e C_a \quad d(Q_c d) = K_e C_a dx$$

$$\left\{ \begin{array}{l} Q(x) d(x) \\ d(Q_c d) = K_a \end{array} \right\} \int_0^x C_{a0} e^{\frac{K_e}{Q_a} dx}$$

$$Q(0) C_d(0)$$

$$Q(x) C_d(x) = Q(0) C_d(0) = K_e C_{a0} \frac{Q_a}{K_a} \left[e^{\frac{K_e x}{Q_a}} - 1 \right]$$

$$C_d(x) = Q(0) C_d(0) + \frac{Q_0 (Q_0 [e^{\frac{K_Q}{K_d} x} - 1])}{Q(x)}$$

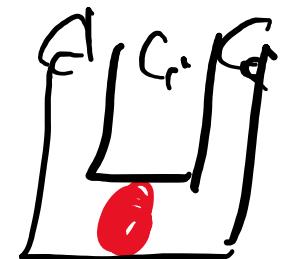
dove $Q(x) = Q(0) - \frac{K_Q}{K_d} (Q_0 Q_0 [e^{\frac{K_Q}{K_d} x} - 1])$

$$K_Q \dot{C}_Q = -K_d (C_d - C_i)$$

$C_i = \phi$ $K_Q C_Q = -K_d (d$ Fisiologica formazione, \rightarrow

$C_i = \phi$ $C_Q \gg C_d$ fisiologica

$C_i \neq \phi$ $C_Q \ll C_d$ calciasi-patologica



$C_i \neq 0$ $C_i = C_a = C_d$ morte 

$C_i \neq 0$ $C_i << C_d$ $C_i << C_a$ patologico - sclerotizz.

$C_i \neq 0$ $C_i << C_d$ $C_i \gg a$ fisiologico - differenza d.
sol.

$C_i \neq 0$ $C_i \gg C_d$ $C_i \gg C_a$ patologico - edema
rit.-rid. circ.

$C_i \neq 0$ $C_i \gg C_d$ $C_i << C_a$ fisiologico - dif. press.
disol.

$$-\frac{d(QCd)}{dx} = K_d (C_d - C_i) \quad \text{Close}$$

$$Q_a \frac{d(C_a)}{dx} = K_a (C_a - C_i)$$

$$-\frac{dQ}{dx} = K_o (C_i - C_d)$$

$$K_a (C_a - C_i) = -K_d (C_d - C_i)$$

$$C_i - C_d = C^*$$

$$-\frac{d(Q_d C_d)}{dx} = -K_d C^* \quad (1)$$

$$Q_e \frac{d(C_e)}{dx} = K_e (C_e - C_i) \quad (2)$$

$$-\frac{d(Q_e)}{dx} = K_e C^* \quad (3)$$

$$K_e (C_e - C_i) = K_d C^* \quad (4)$$

Eq. 3.

$$-\frac{dQ}{dx} = k_0 C^* \quad \Rightarrow \quad -dQ = k_0 C^* dx$$

$$C^* \approx \text{const} \quad - \int_{Q(0)}^{Q(x)} dQ = k_0 C^* \int_0^x dx$$

$$-Q(x) + Q(0) = k_0 C^* x$$

$$Q(x) = Q(0) - k_0 C^* x$$

Eq. 1

$$-\frac{d(Q_c d)}{dx} = -k d C^*$$

$$+ d(Q_c d) = +k d C^* dx$$

$$+\int_{Q(x)d(x)}^{Q(0)d(0)} d(Q_c d) = +k d C^* \int_0^x dx$$

$$Q(x)C_d(x) - Q(0)C_d(0) = K d C^* x$$

$$C_d(x) = \frac{[Q(0)C_d(0) - K d C^* x]}{[Q(0) - K_0 C^* x]}$$

Cq. 2.

$$Q_a \frac{dc_e}{dx} = k_e (c_e - c_i) \Rightarrow k_e (c_a - c_i) = k_d c^*$$

$$Q_a \frac{dc_e}{dx} = k_d c^*$$

$$Q_a dc_e = k_d c^* dx$$

$$dc_e = \frac{k_d}{Q_a} c^* dx$$

$$\int_{c_e(0)}^{c_e(x)} dc_e = \frac{k_d}{Q_a} c^* \int_0^x dx$$

$$\left. \begin{aligned} c_e(x) - c_e(0) &= \frac{k_d}{Q_a} c^* x \\ c_e(x) &= c_e(0) + \frac{k_d}{Q_a} c^* x \end{aligned} \right\}$$

$$c_a(x) - c_a(0) = \frac{k_d}{Q_a} c^* x$$

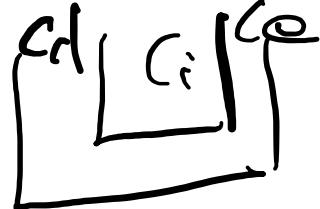
$$\text{Se } C_i = \phi \quad C^* = -C_d \quad K_C \cdot C_d = -K_d \cdot C_d$$

Se $C_e \neq C_d$ condizione fisiologica formazione renale

$C_i = \phi$ $C_e >> C_d$ patologiche edema renale

$C_i = \phi$ $C_e \ll C_d$ patologiche sangue che si basifica

$C_i = \phi$ $C_e = C_d$ morte



$C_i \neq 0$ $C_e >> C_i$ $C_d >> C_i$ sclerof. nefr. pat.

$C_e \gg C_i$ $C_d \ll C_i$ diab. pat

$C_e \ll C_i$ $C_d >> C_i$ placid. sangue nef

$C_e \ll C_i$ $C_d \ll C_i$ edema